

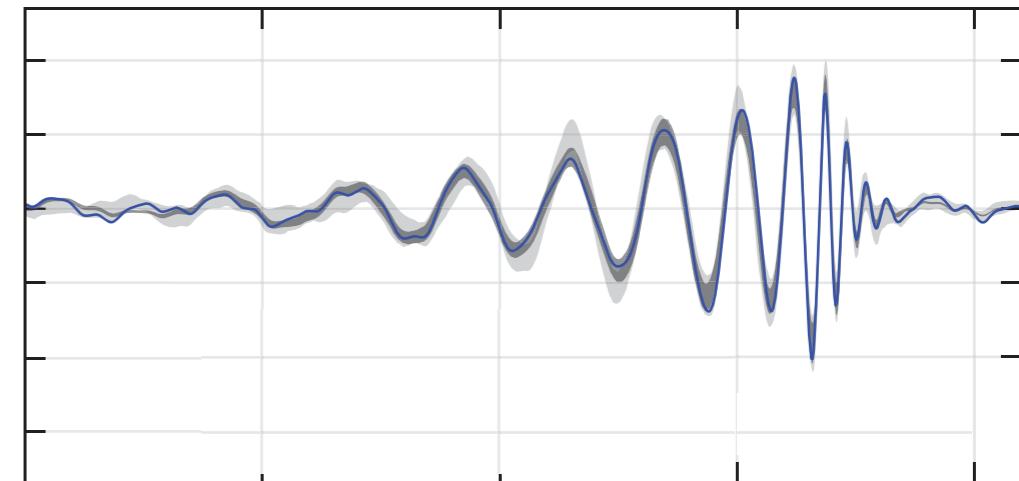
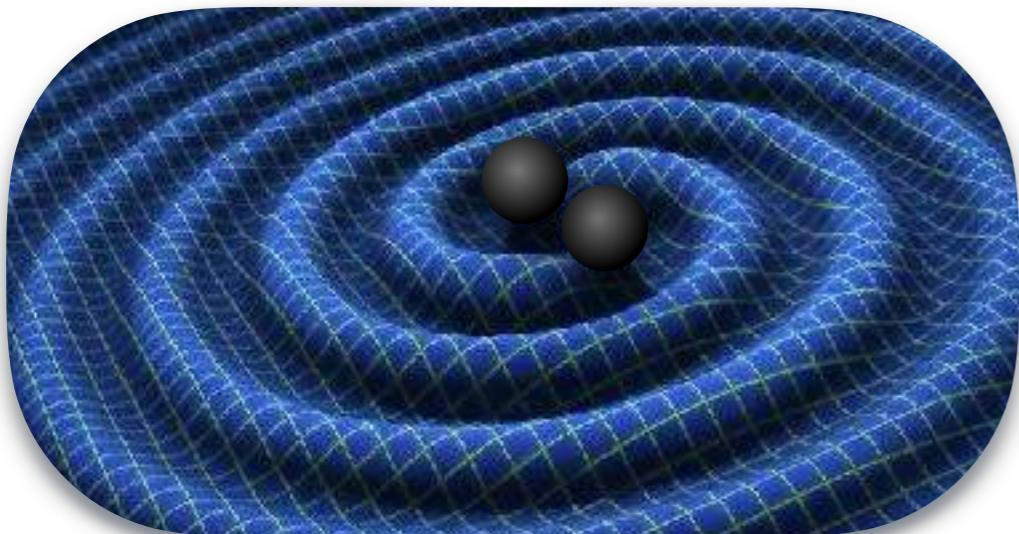


École Doctorale d'Astronomie & Astrophysique
d'Île-de-France



la Valse Hélicoïdale des Trous Noirs

How to make spacetime vibrate with dancing black holes ?

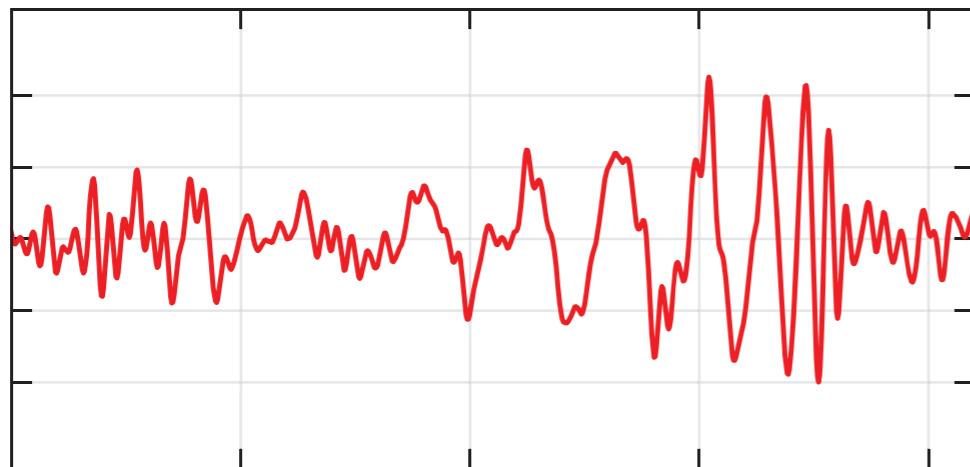
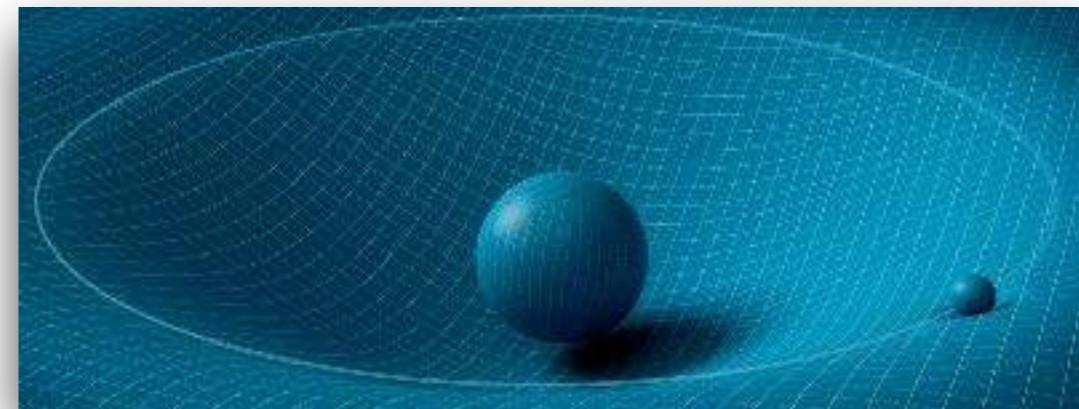


— Paul Ramond —

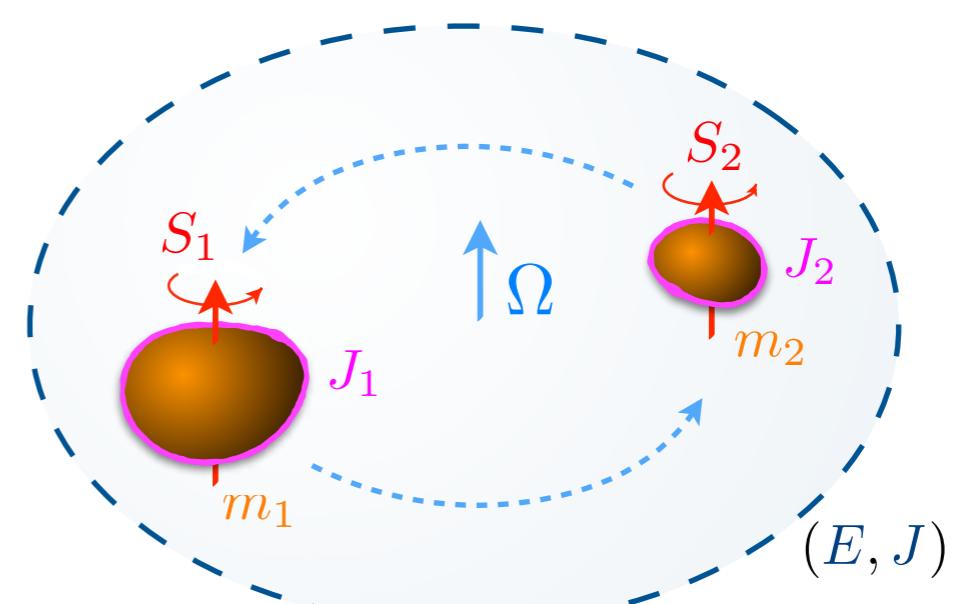
Laboratoire Univers et THéories

Summary

1. General Relativity



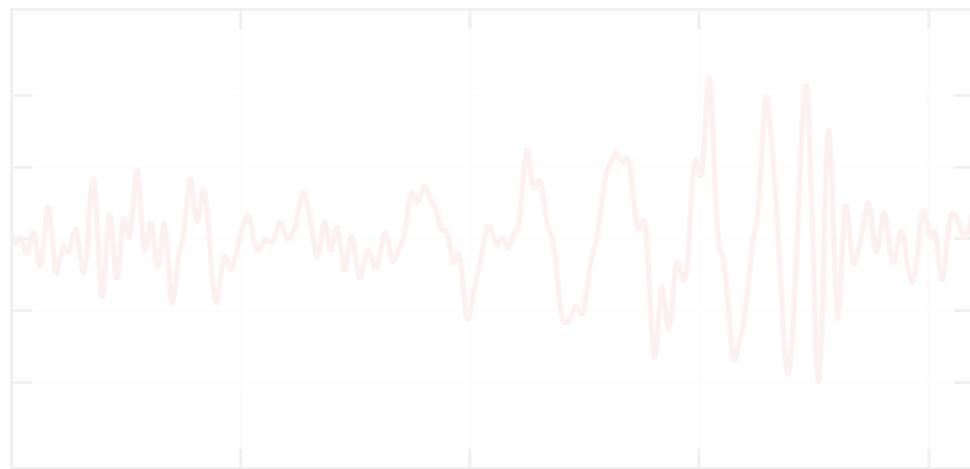
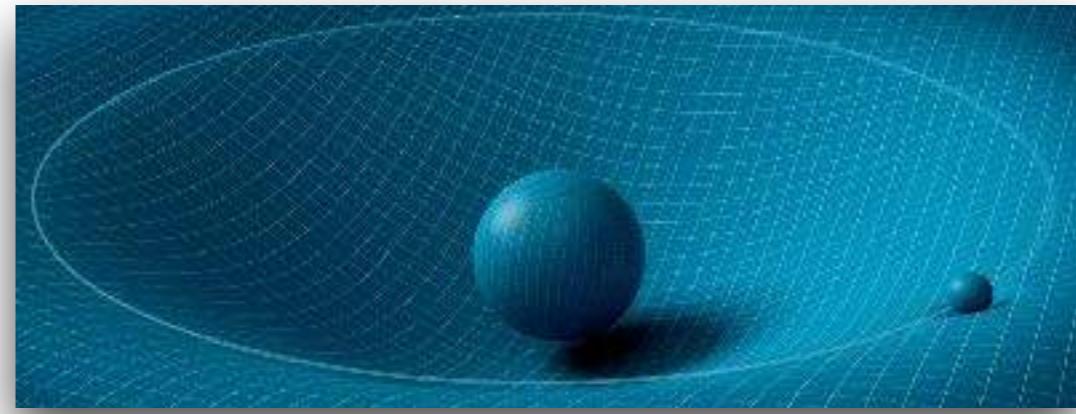
2. Gravitational Waves



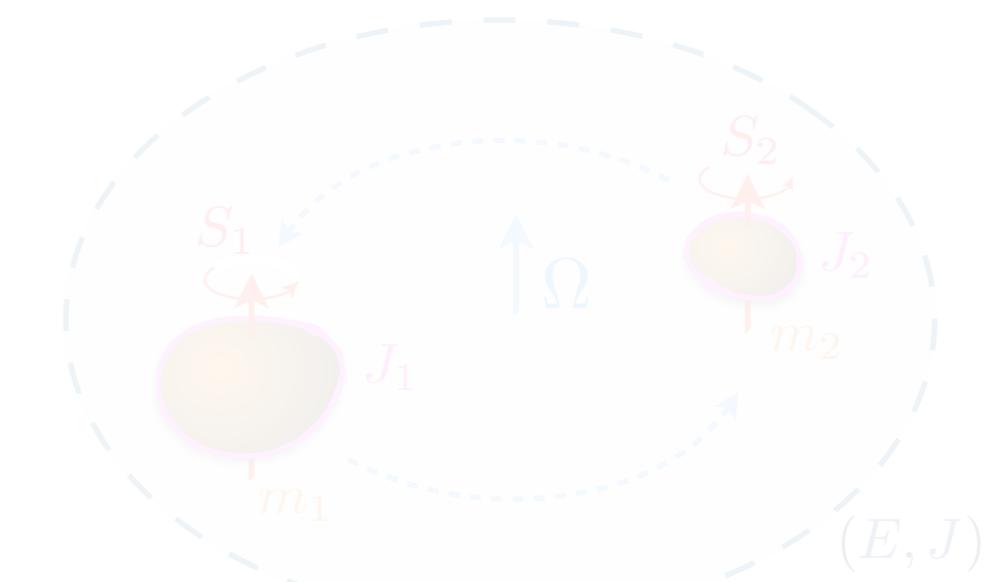
3. My PhD

Summary

1. General Relativity



2. Gravitational Waves



3. My PhD

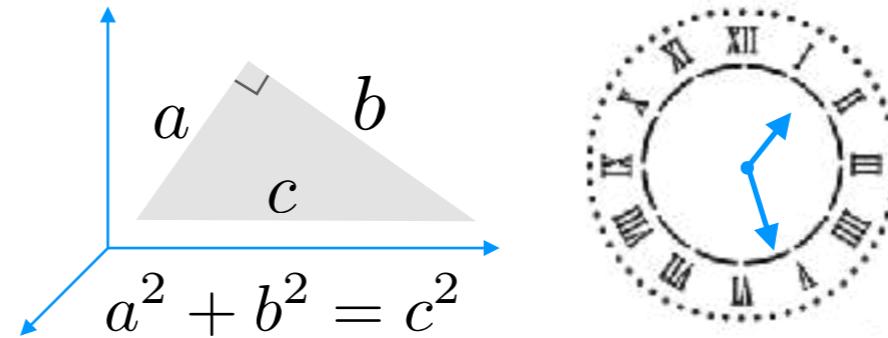
General Relativity

- Theory of **Space, Time and Gravitation**
- Formulated by **A. Einstein** between 1915 and 1918
- Never proved wrong (so far), **tested in strong et weak fields**
- Daily life application : **GPS, satellites & interplanetary travel**
- Contains **newtonian gravitation** and **special relativity**
- Corrects : **precession** of elliptic orbits, **time delay** of light, ...
- New predictions : **black holes, expansion of the Universe,...**

And Gravitational Waves !

Newtonian Gravity

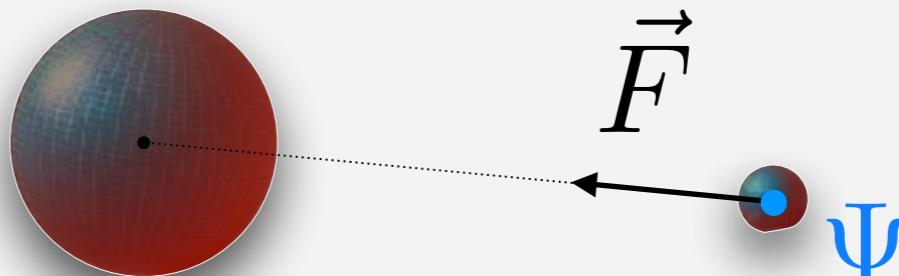
3D **euclidean** space
1D **universal** time



Gravitational Force

$$\vec{F} \propto \vec{\nabla} \Psi$$

Mass density ρ



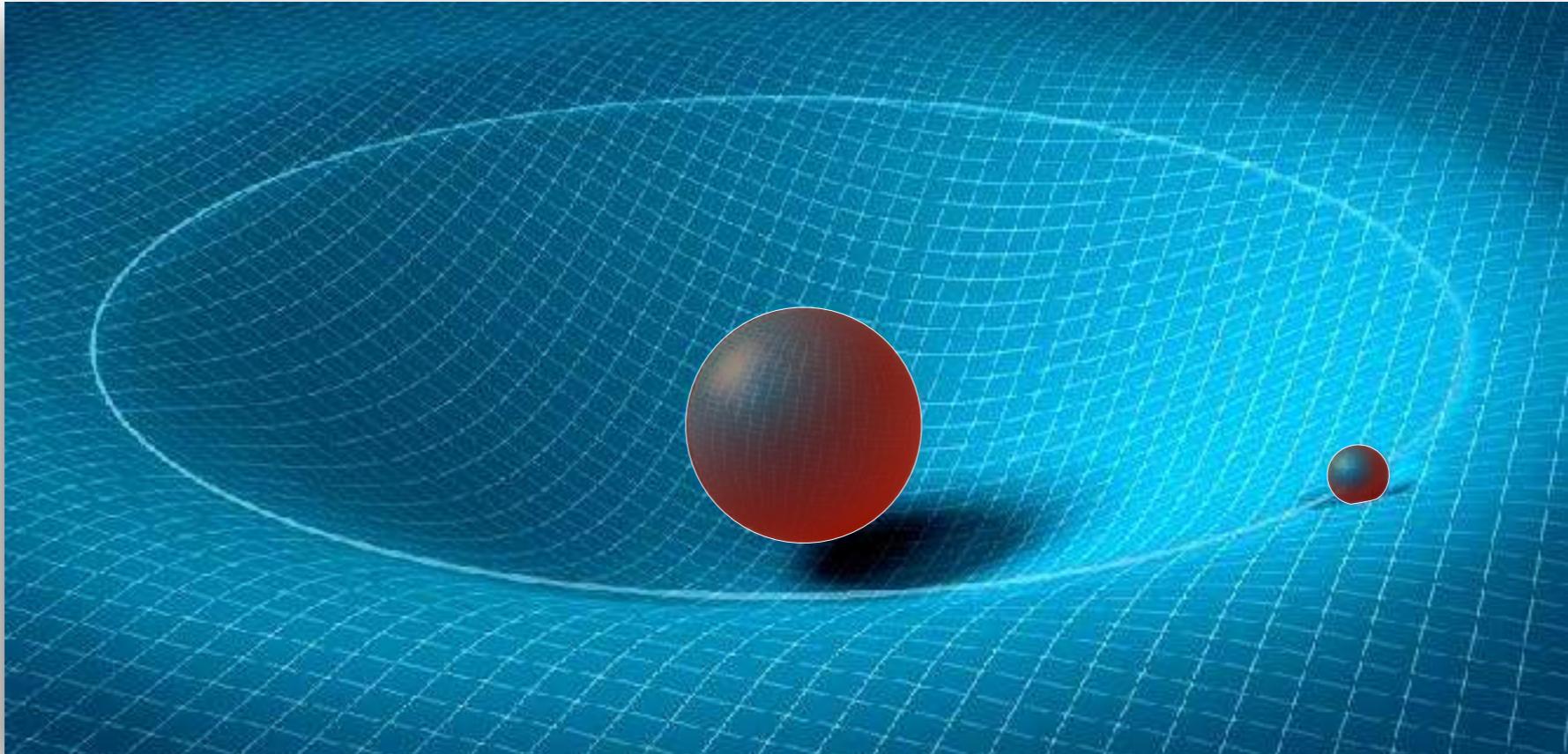
Gravitational field

Poisson Equation

$$\Delta \Psi = 4\pi G \rho$$

General Relativity

Curved 4D Spacetime → g_{ab}
by mass/energy → T_{ab}

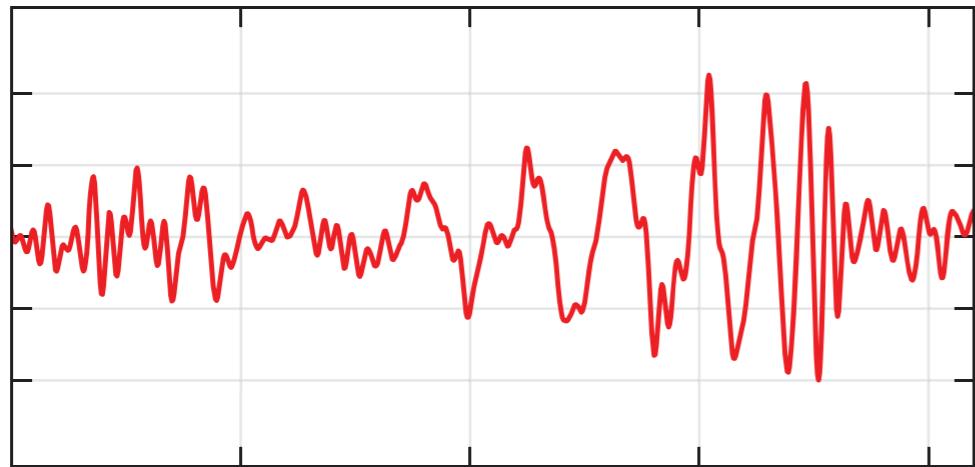


Einstein Equation

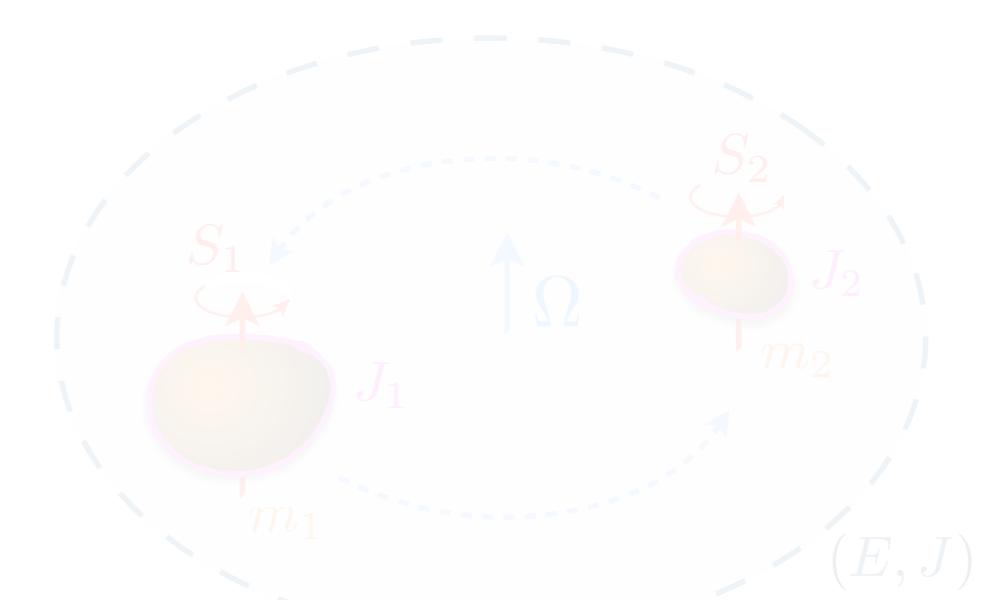
$$G_{ab} = 8\pi G T_{ab}$$

Summary

1. General Relativity



2. Gravitational Waves



3. My PhD

Gravitational Waves (GW) : theory

$$\begin{array}{lcl} \text{Flat spacetime} & \longrightarrow & g_{ab} = \eta_{ab} \\ + \text{small perturbation} & \longrightarrow & g_{ab} = \eta_{ab} + h_{ab} \end{array}$$

... plug in Einstein Equations ...

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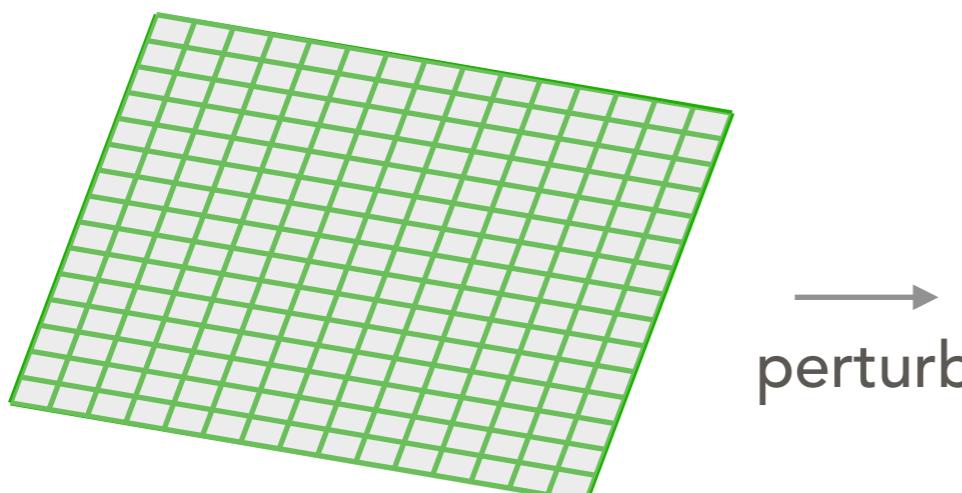
Wave Equation $\square \bar{h}_{ab} = -16\pi G \bar{T}_{ab}$

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GW : astrophysical sources

Order of magnitude

$$h \sim 10^{-21} \left(\frac{M}{10M_{\odot}} \right) \left(\frac{100 \text{Mpc}}{R} \right) \left(\frac{v_a}{c} \right)^2$$

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$h \sim 10^{-21}$

For a typical system

→ of a few
stellar masses

within the
local group

non-spherical
and **relativistic**

GW : astrophysical sources

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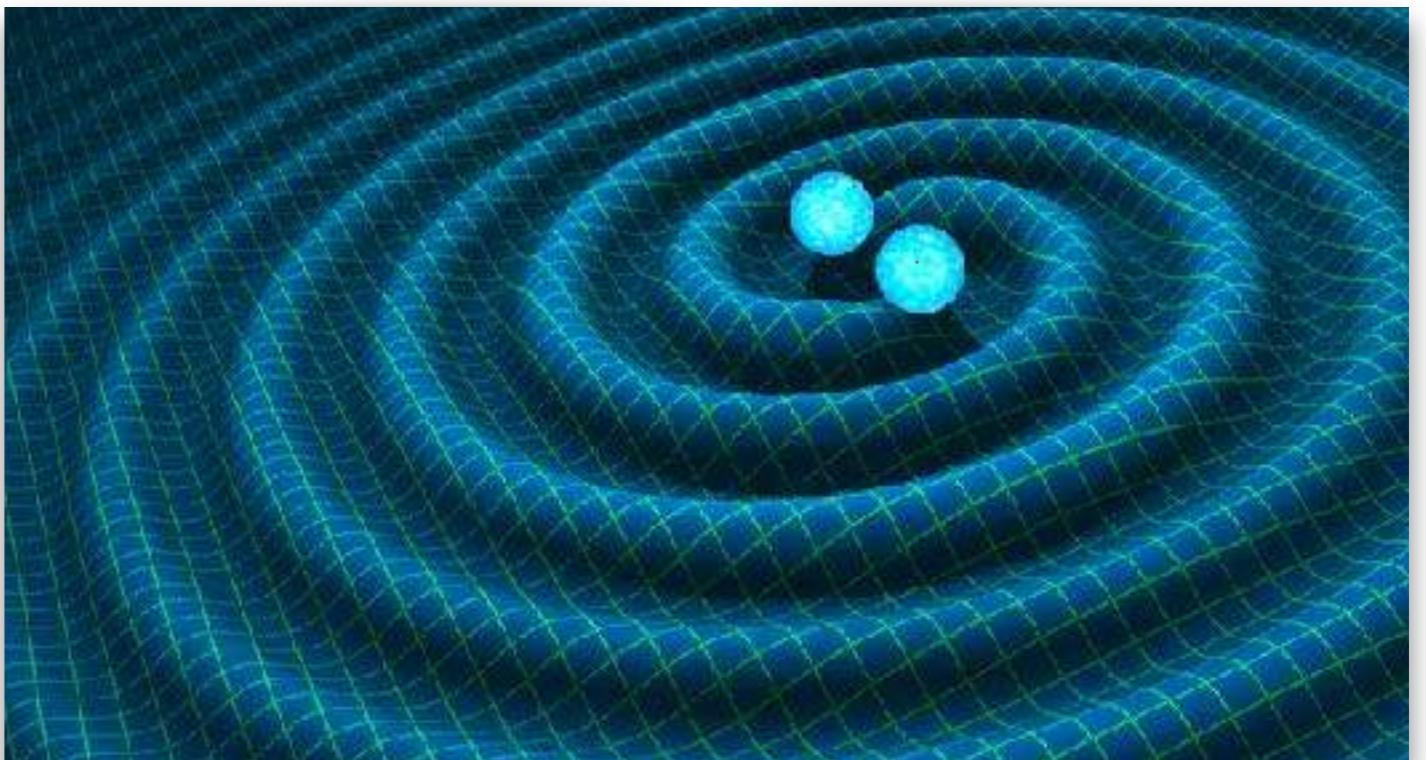
For a typical system

→ of a few stellar masses within the local group non-spherical and relativistic

Most promising GW source :

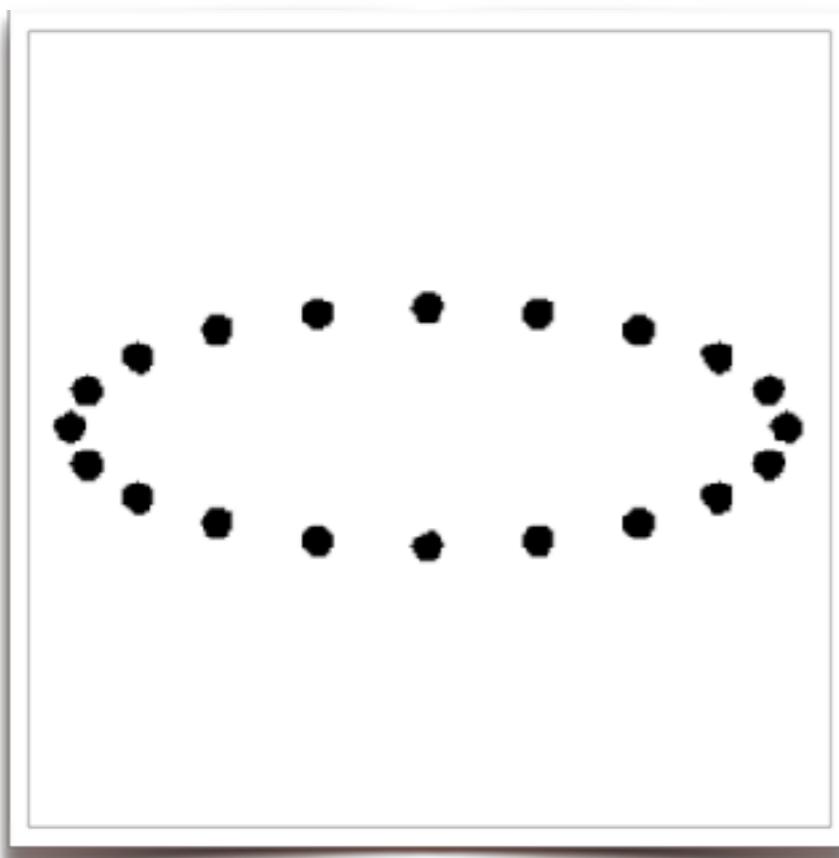
Binary system of Compact Objects

(Black Holes or Neutron Stars)

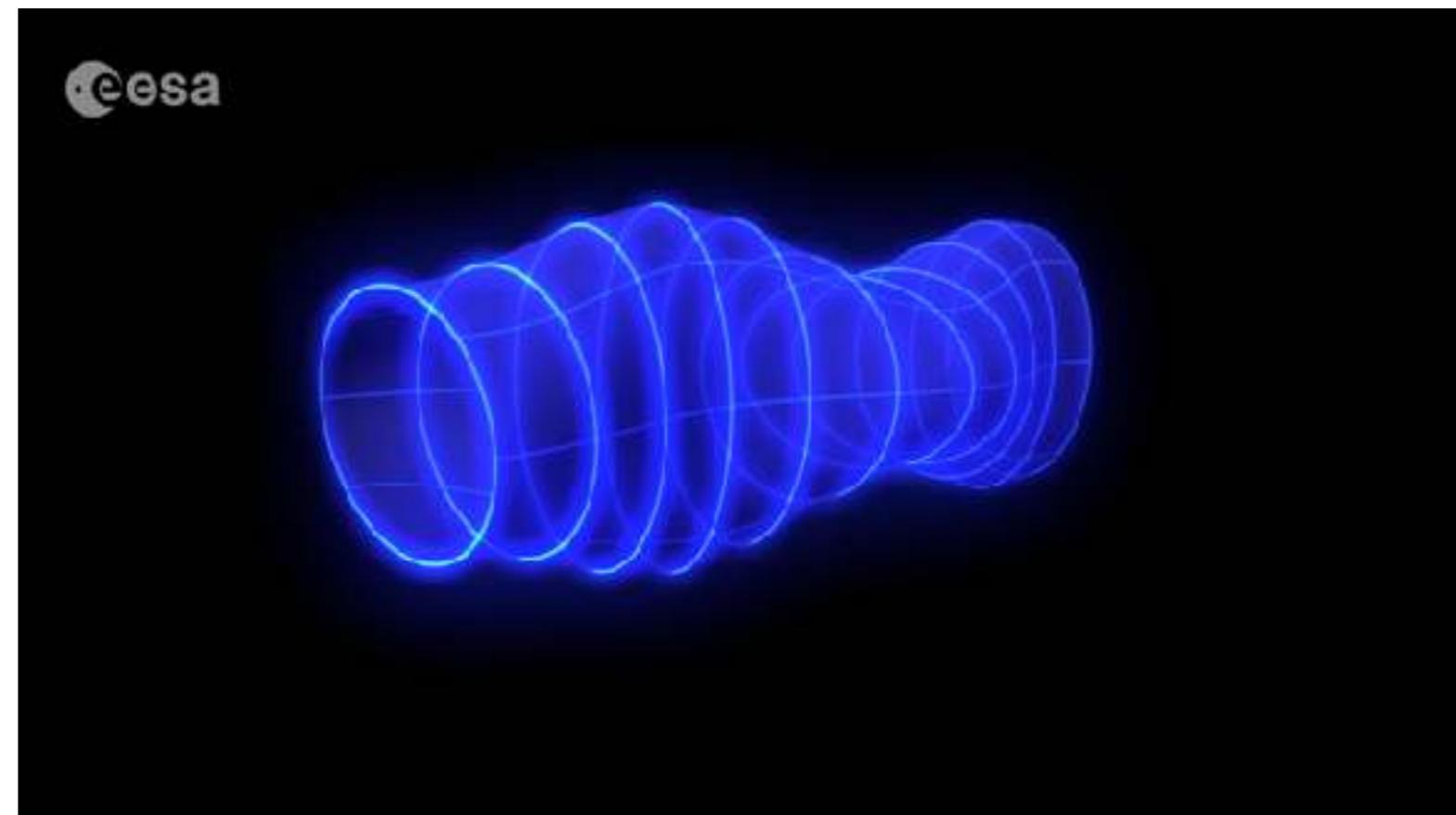


GW : interactions with matter

**Effect of a GW
on ring of particles
(travelling perpendicularly)**



**Effect of a GW on multiple rings
(travelling perpendicularly)**



GW : interactions with matter

Effect of a GW on Earth (vastly exaggerated)



GW : ground based detectors

LIGO and VIRGO
Michelson Interferometers

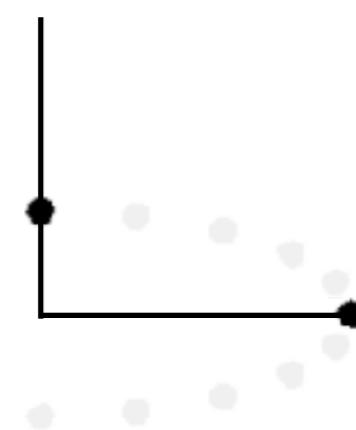


GW : ground based detectors

LIGO and VIRGO
Michelson Interferometers



3-4 km vacuum tunnels with laser beam bouncing off of mirrors

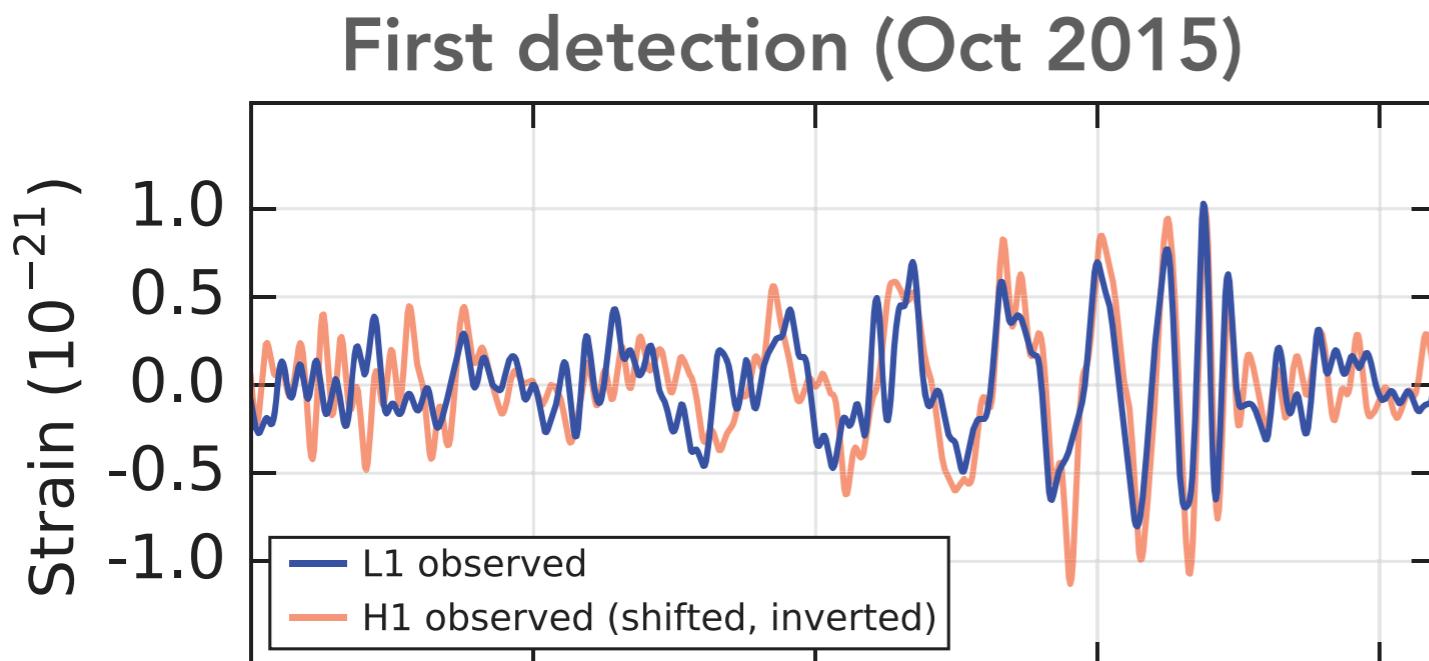


Arm length variation for typical OG

$$\Delta L \approx 4 \cdot 10^{-19} \text{ m}$$

*Earth-Moon distance
with 0.1 Å accuracy...*

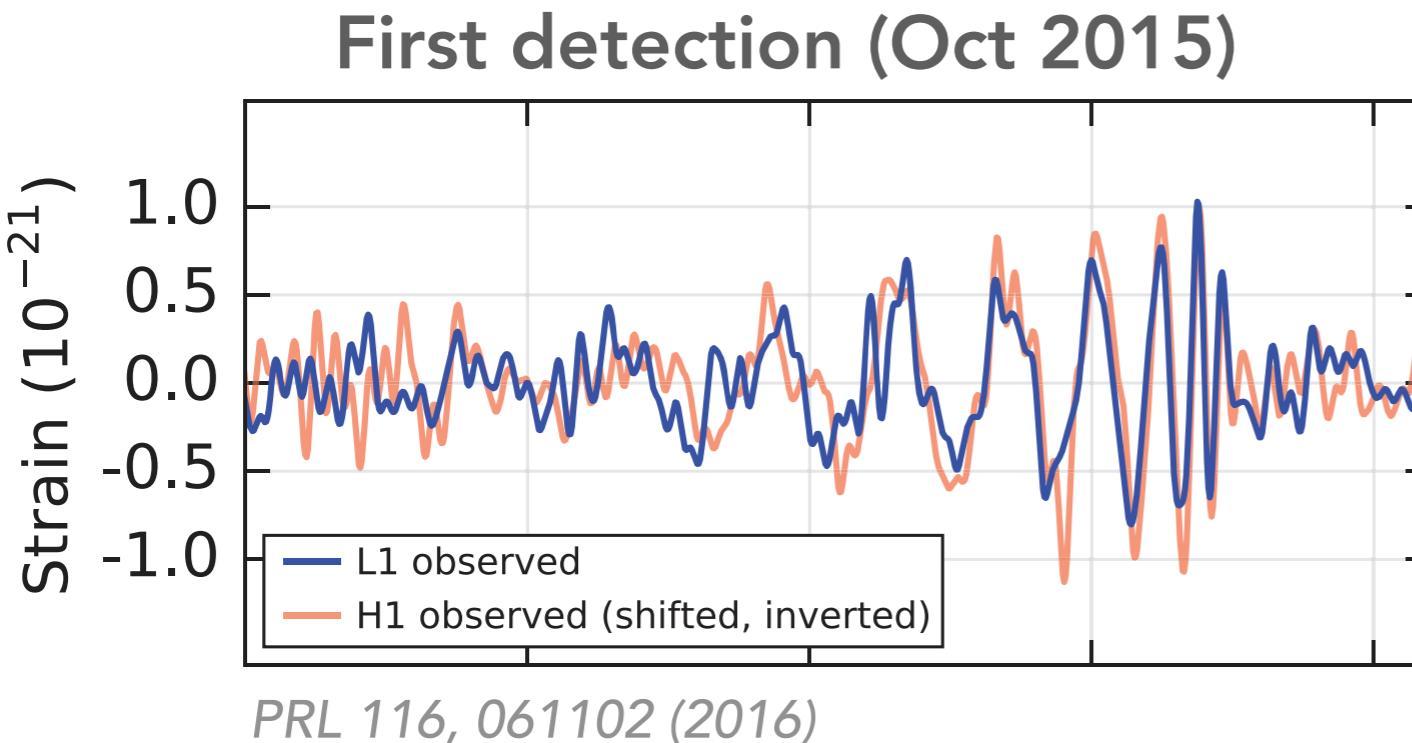
GW : first detections



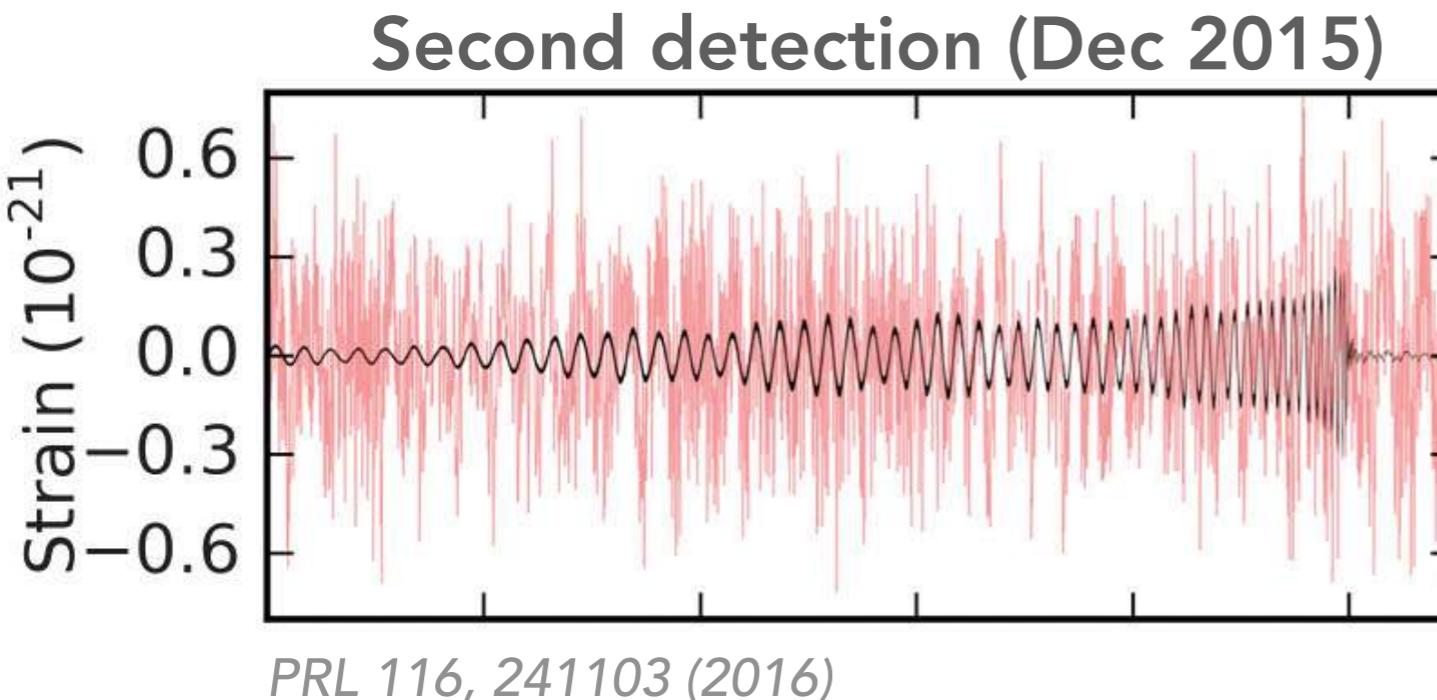
PRL 116, 061102 (2016)

How to infer
physical parameters
from the GW ?

GW : first detections



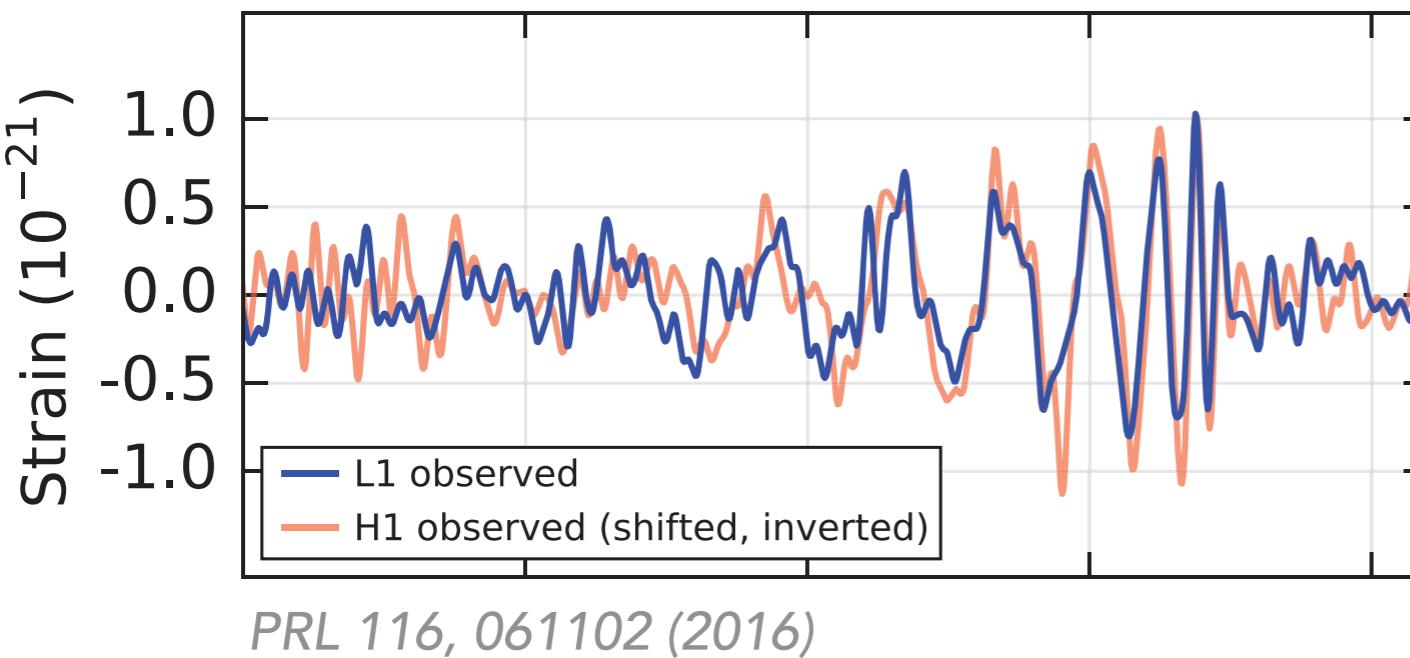
How to infer
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How to extract the
GW from the noise ?

GW : first detections

First detection (Oct 2015)

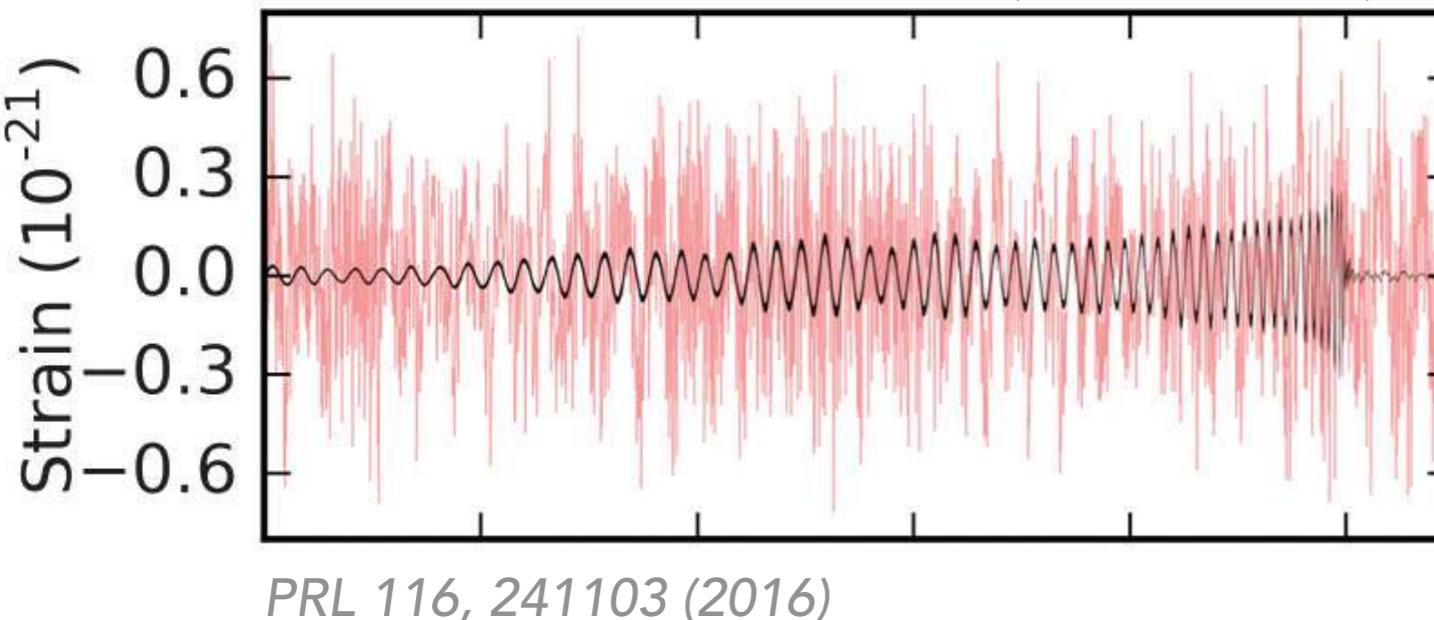


How to infer
physical parameters
from the GW ?



*Using
GW templates !*

Second detection (Dec 2015)



How to extract the
GW from the noise ?



GW : templates

Ex : for a binary system of two black holes

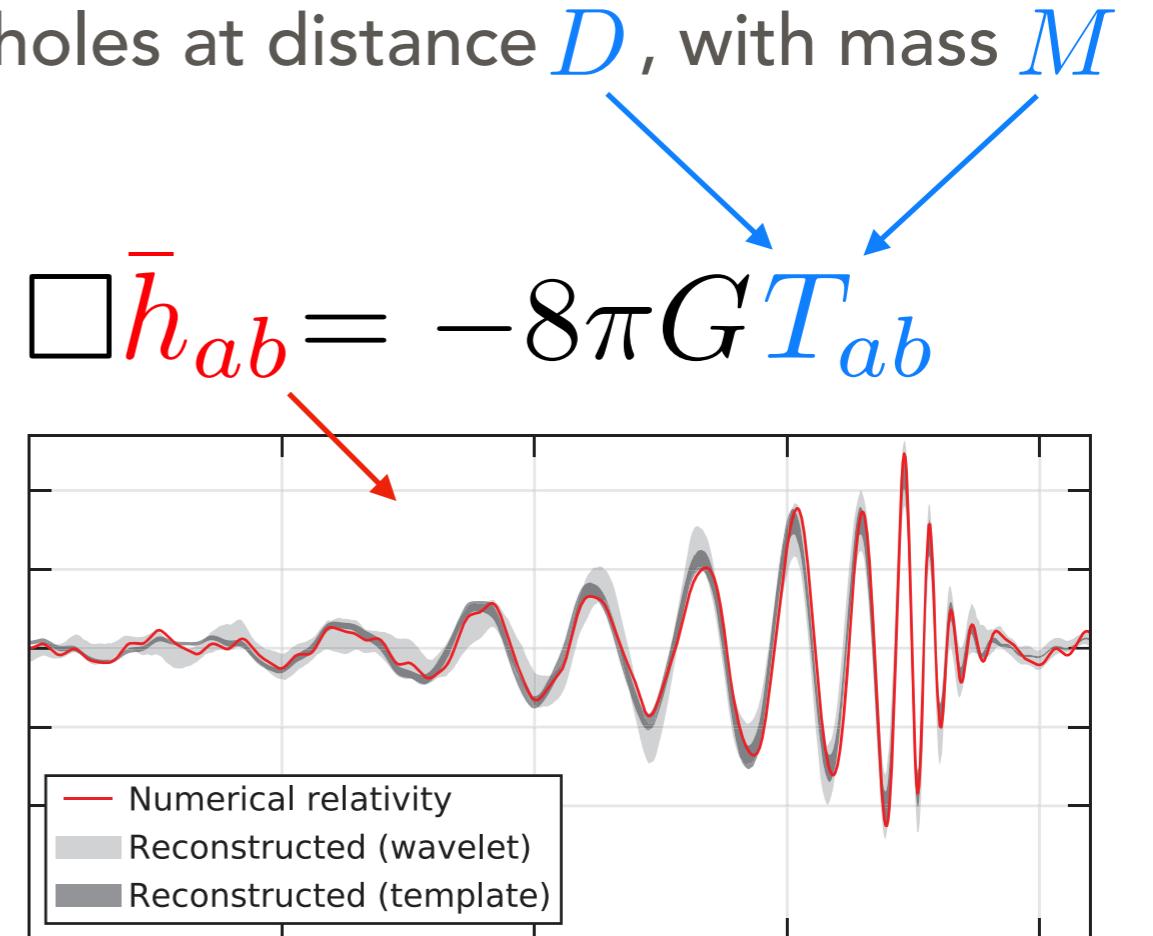
Step 1. Model a binary system of black holes at distance D , with mass M

GW : templates

Ex : for a binary system of two black holes

Step 1. Model a binary system of black holes at distance D , with mass M

Step 2. Construct GW template :
solve GW equation for this system



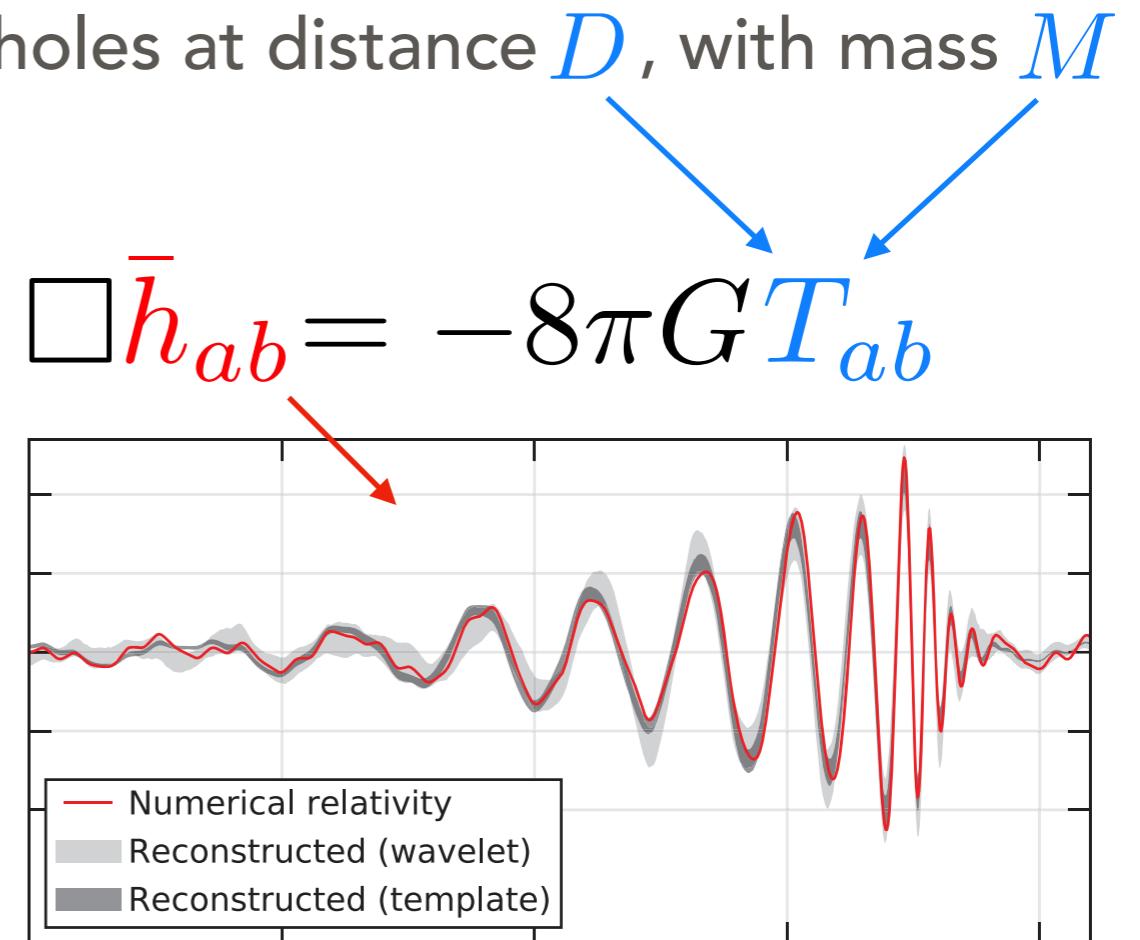
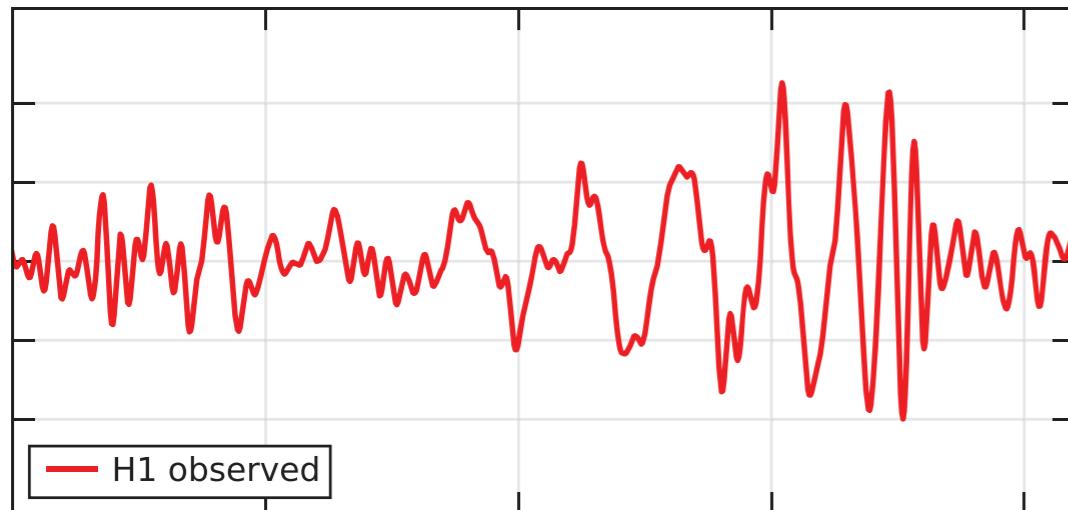
GW : templates

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Step 1. Model a binary system of black holes at distance D , with mass M

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Step 3. Match detector signal
with template bank to detect



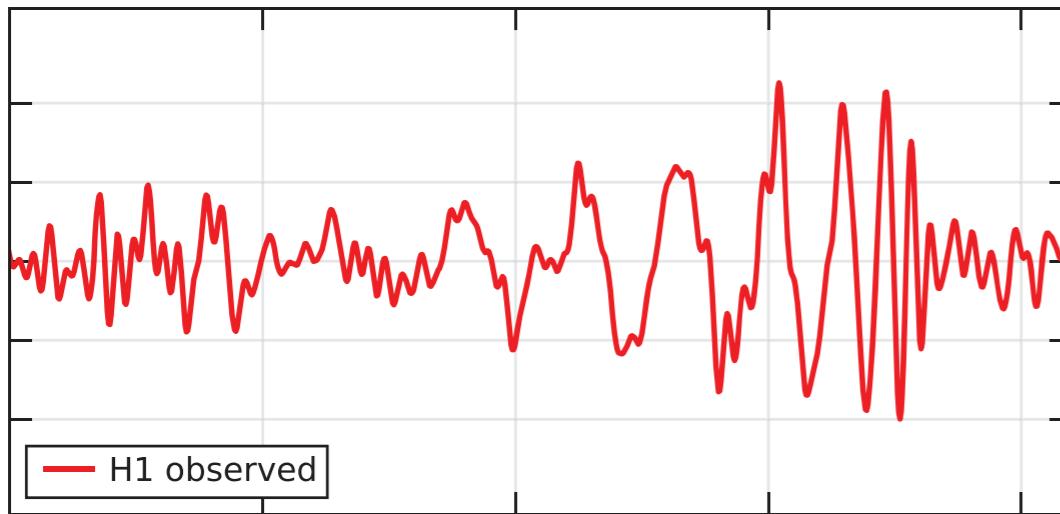
GW : templates

Ex : for a binary system of two black holes

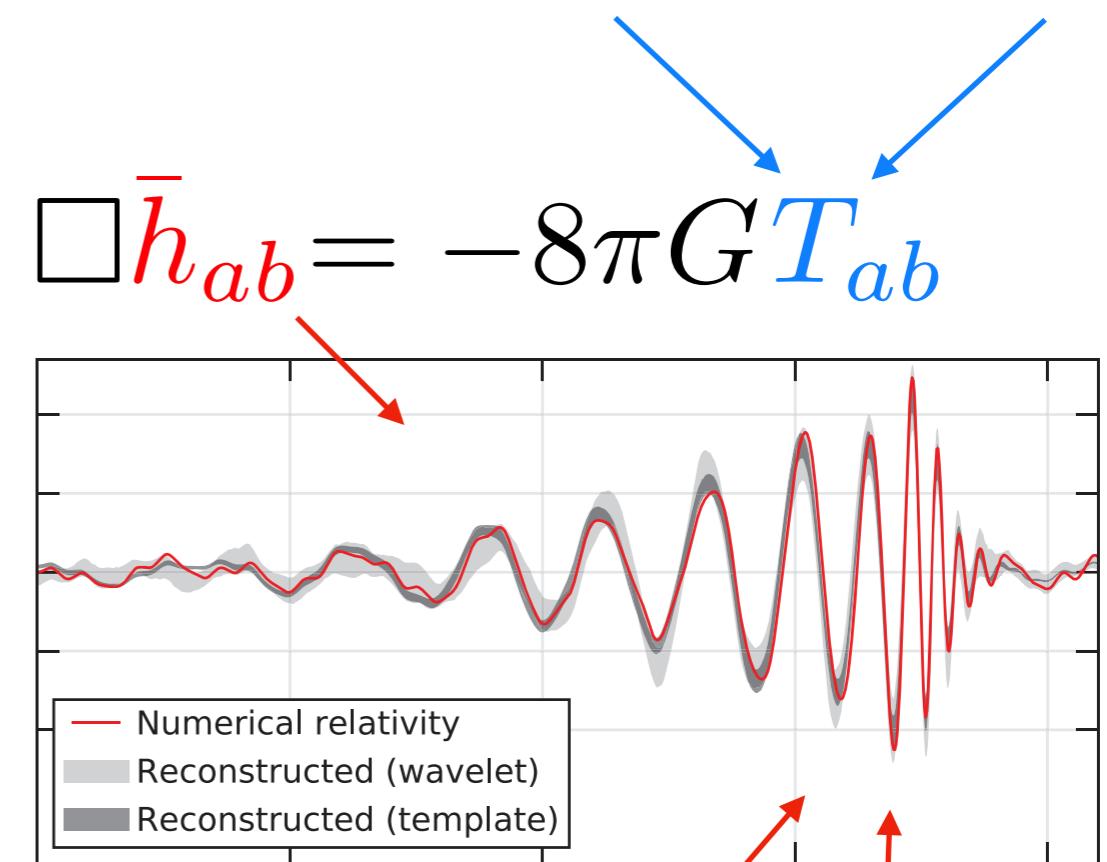
Step 1. Model a binary system of black holes at distance D , with mass M

Step 2. Construct GW template :
solve GW equation for this system

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Step 4. Match with best
template to extract source data

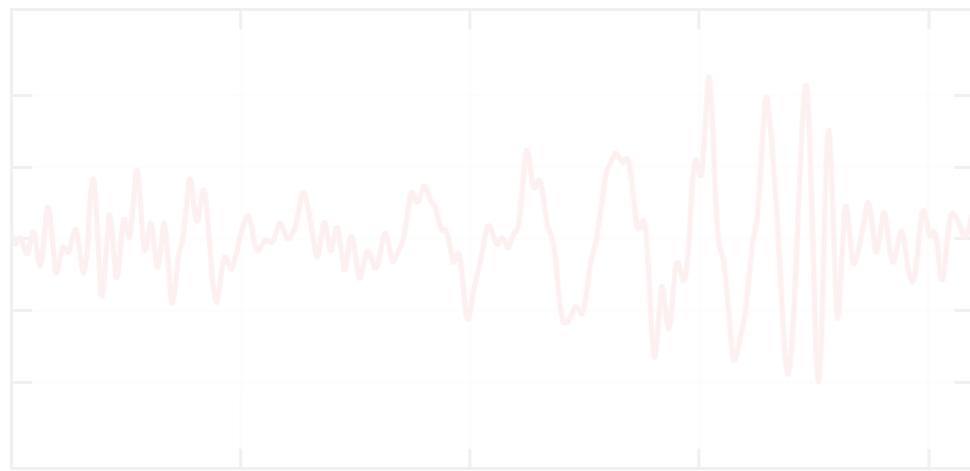


$$D = \frac{5c}{24\pi^2} \frac{\dot{f}}{f^3 A}$$

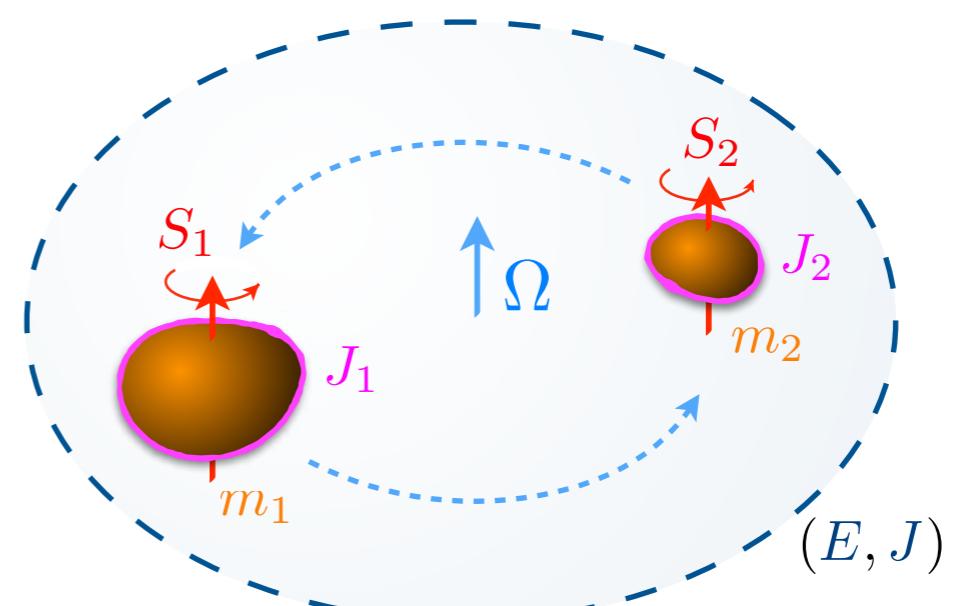
$$M = \left[\frac{5}{96} \frac{c^5}{G\pi^{8/3}} \frac{\dot{f}}{f^{11/3}} \right]^{3/5}$$

Summary

1. General Relativity



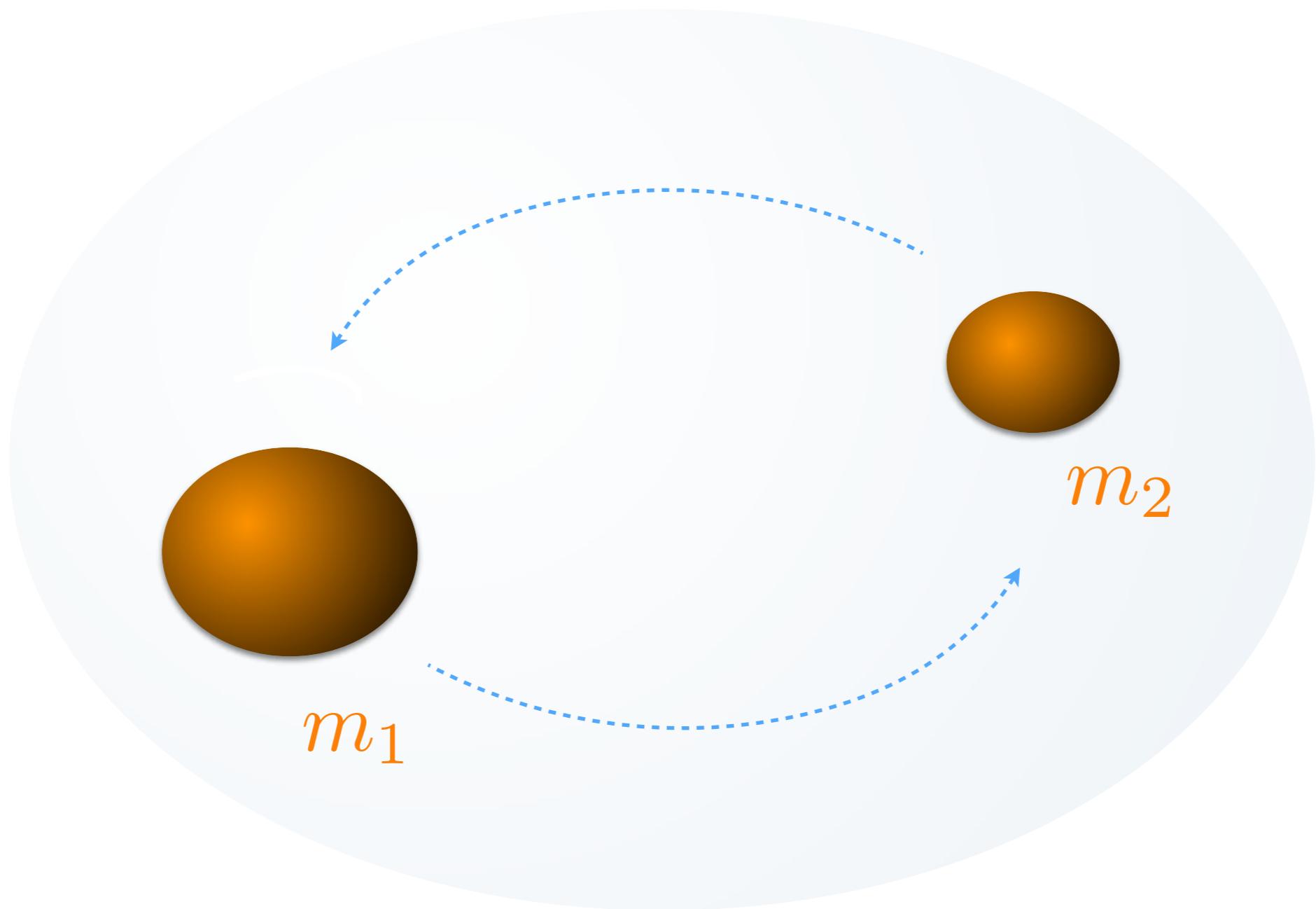
2. Gravitational Waves



3. My PhD

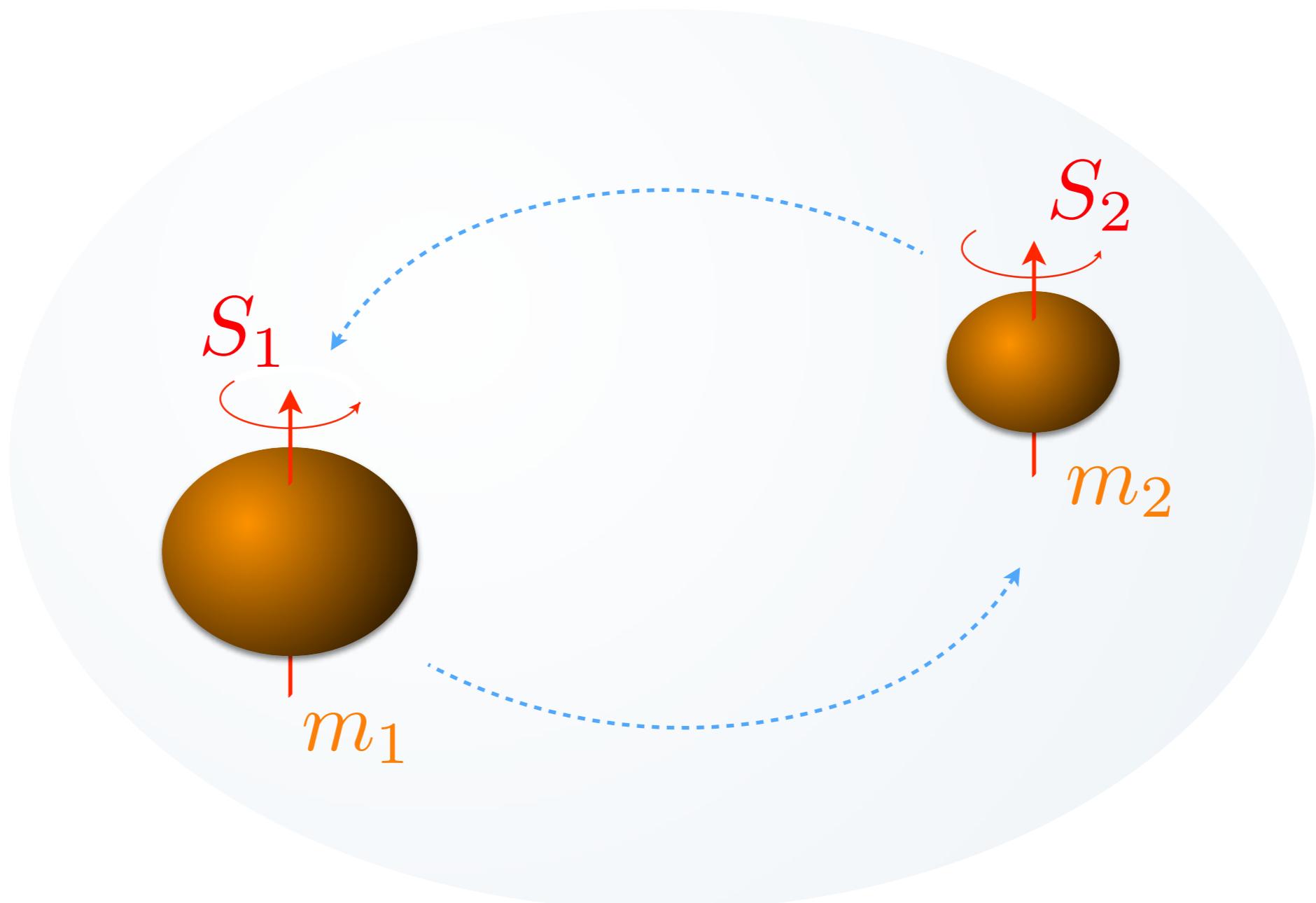
Model of binary system 1.0

Step 1. Refined model of binary systems of compact objects (NS or BH)



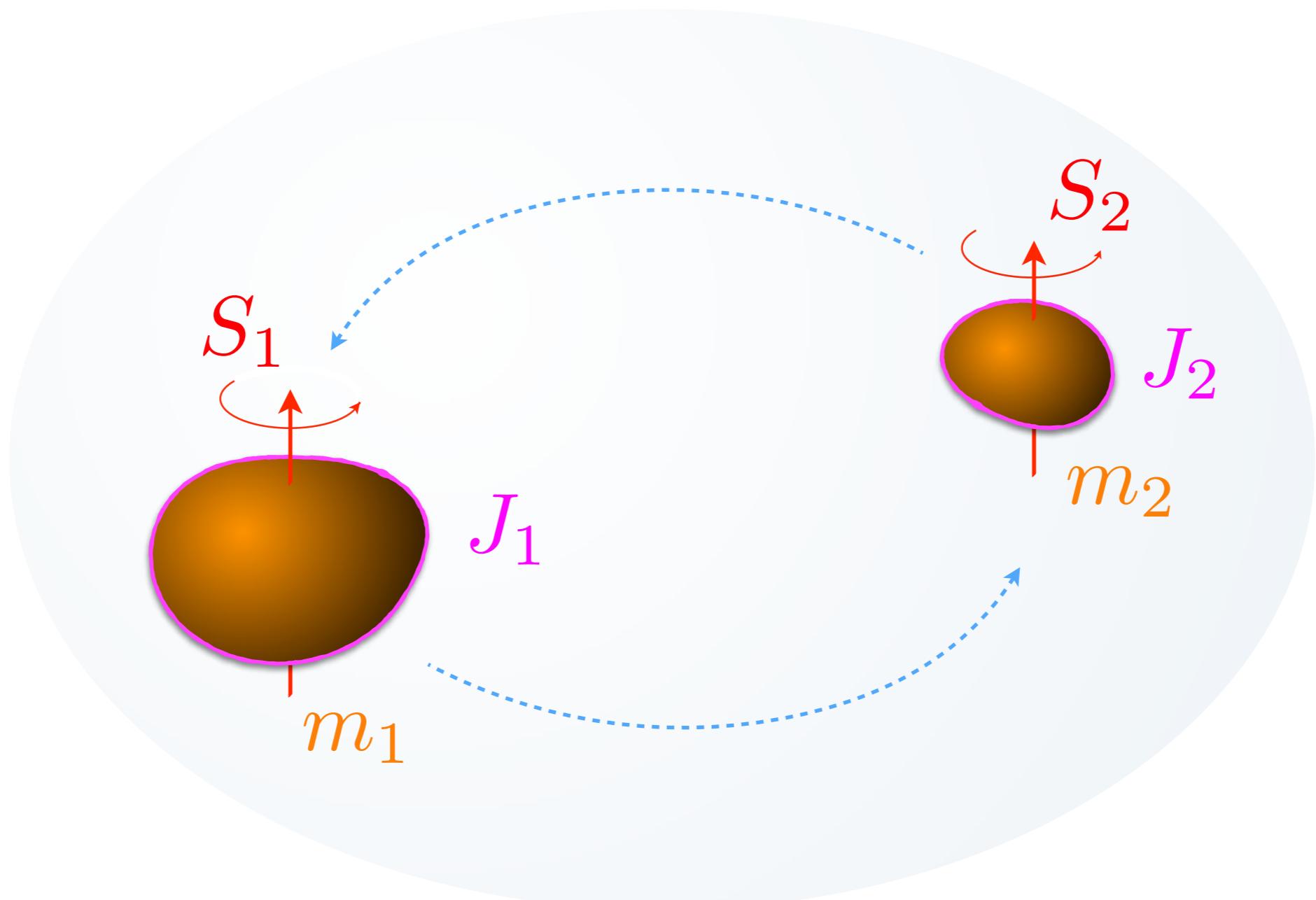
Model of binary system 2.0

Step 1. Refined model of binary systems of compact objects (NS or BH)



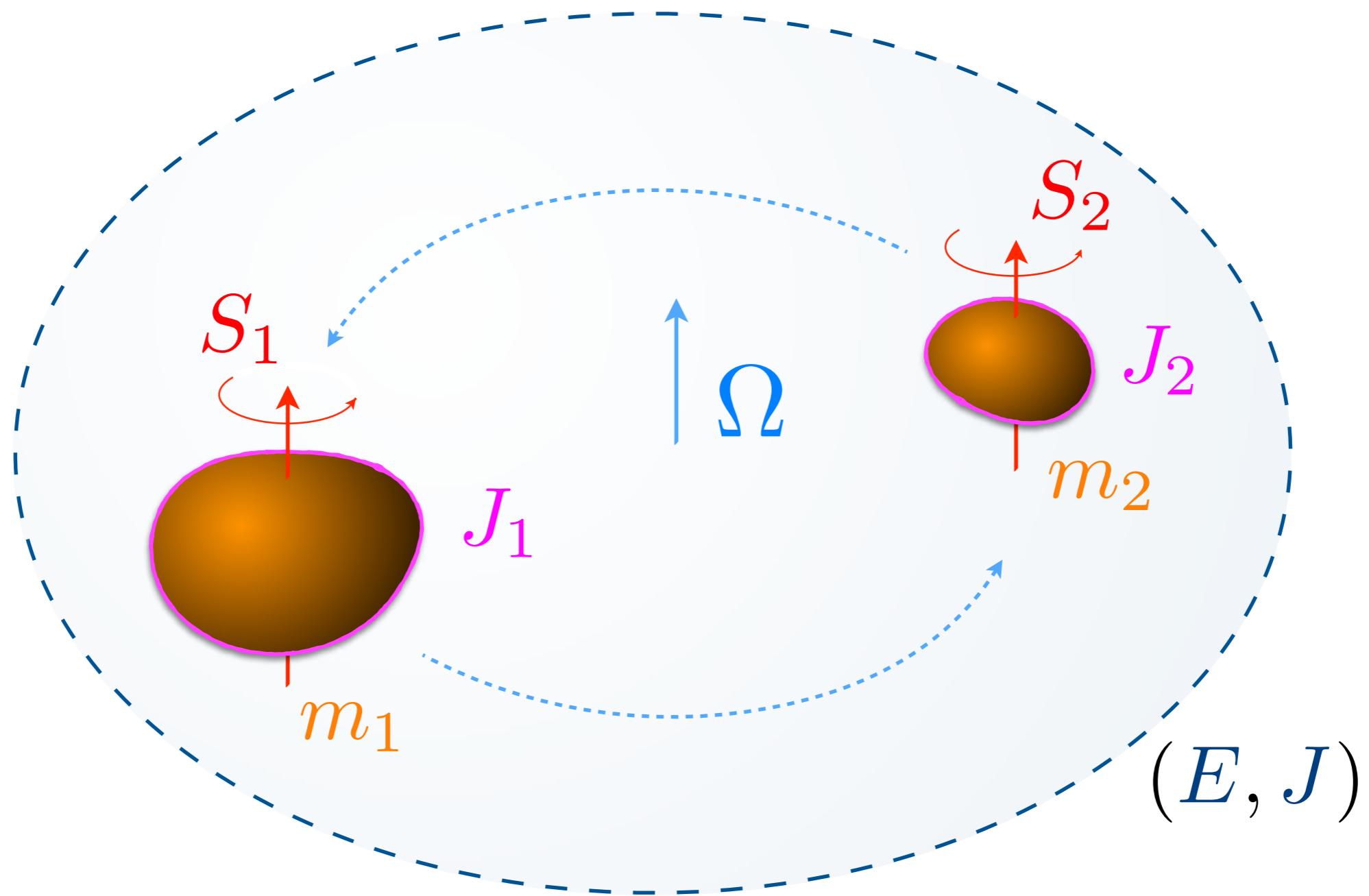
Model of binary system 3.0

Step 1. Refined model of binary systems of compact objects (NS or BH)



My PhD : relate global and local properties

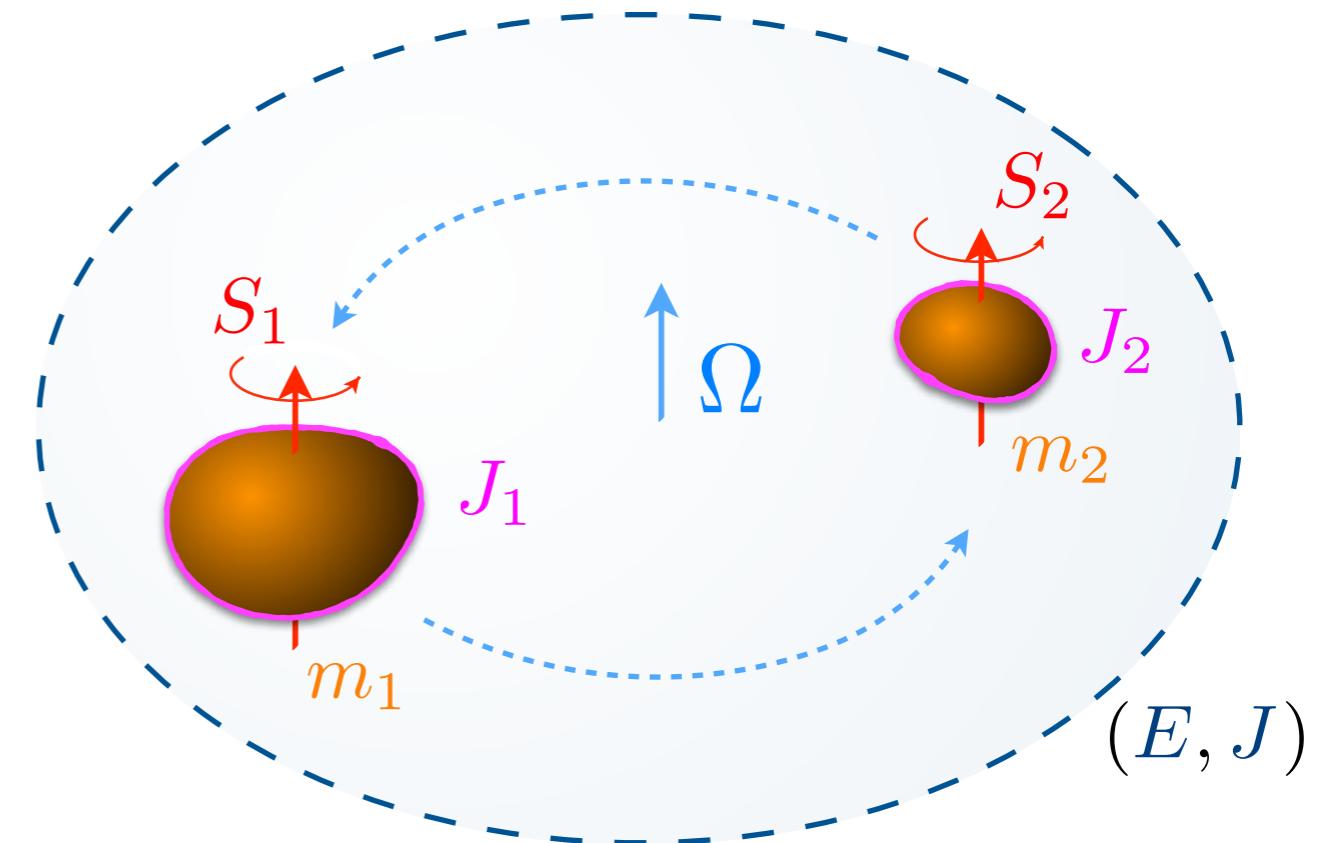
Step 1. Refined model of binary systems of compact objects (NS or BH)



First law of black hole mechanics

Equation relating
 (E, J, Ω) to (m_i, S_i, J_i)

**First law of
black hole mechanics**



$$\delta M - \Omega \delta J = \sum_{i=1,2} [|k| \delta m_i] + [\nabla k \delta S_i] + [\nabla \nabla k \delta J_i]$$

2012 2018 2020
(done this year) (if all goes well!)

Thank you !

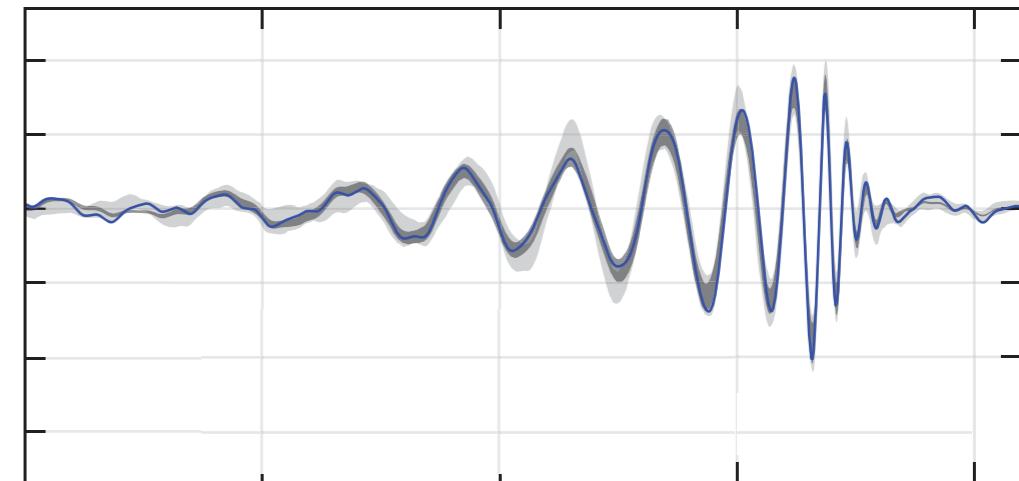
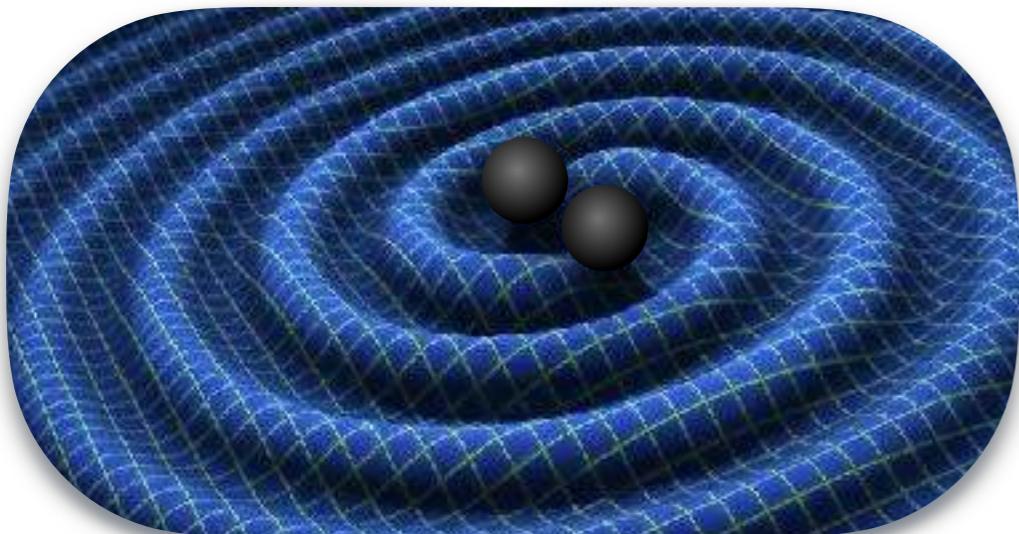


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